

# Shape Optimization Approach to the Bernoulli Problem: A Lagrangian Formulation

Julius Fergy T. Rabago<sup>1</sup> and Jerico B. Bacani<sup>2</sup>

Department of Mathematics and Computer Science  
College of Science, University of the Philippines Baguio  
Governor Pack Road, Baguio City 2600, Philippines  
Email: <sup>1</sup>jfrabago@gmail.com, <sup>2</sup>jicderivative@yahoo.com

## Abstract

The exterior Bernoulli free boundary problem is reformulated into a shape optimization setting by tracking the Dirichlet data. The shape derivative of the corresponding cost functional is established through a Lagrangian formulation coupled with the velocity method. A numerical example using the traction method or  $H^1$  gradient method is also provided.

**2010 Mathematics Subject Classification:** Primary 35R35; Secondary 35N25, 49K20, 49M30.

**Keywords:** Bernoulli free boundary problem, overdetermined boundary value problem, shape derivative, Lagrange method, minimax formulation.

**Note:** The full paper has the following citation: Julius Fergy T. Rabago, and Jerico B. Bacani, "Shape Optimization Approach to the Bernoulli Problem: A Lagrangian Formulation," IAENG International Journal of Applied Mathematics, vol. 47, no. 4, pp. 417-424, 2017.